

Labor Economics, Week 4  
Wage inequality, labor demand,  
Competitive model, and monopsony

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## Takeaways for week 3 - Labor demand

### 1. Estimating labor demand

- ▶ Regressions of relative wages on relative labor supply (possibly with instrument).
- ▶ To assess the impact of migration or technical change on inequality.
- ▶ Motivated by the competitive model of wage setting.

### 2. Minimum wages

- ▶ The competitive model predicts that increasing minimum wages lowers employment.
- ▶ Studies use difference-in-differences design across US states to estimate this effect.
- ▶ Most find no effect on employment.

### 3. Monopsony

- ▶ This has renewed interest in monopsony models of labor demand.
- ▶ An employer has monopsony power if their labor supply is not infinitely responsive.
- ▶ Monopsony power implies a non-monotonic relationship between minimum wages and employment.

# Roadmap

Estimating labor demand

Minimum wages

Monopsony

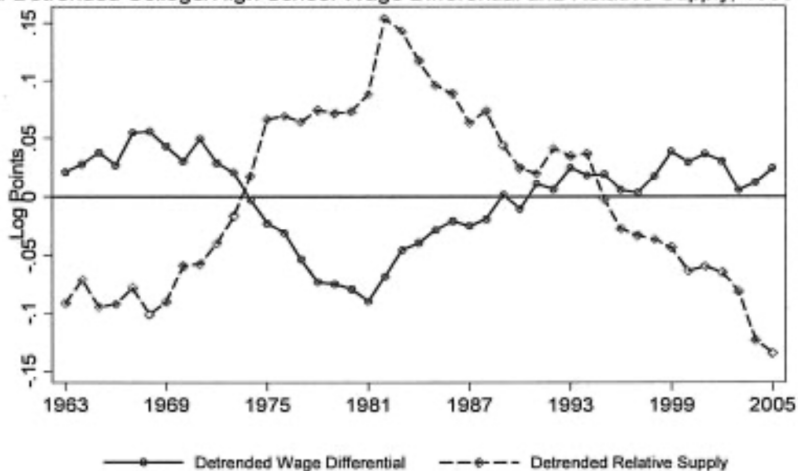
- ▶ Earned income is the largest source of household incomes (ca. 60%).
- ▶ ⇒ Wage inequality matters for income inequality.
- ▶ Many factors might affect the wage distribution:
  1. Labor **supply** of different “types” of workers
    - 1.1 Education
    - 1.2 Demographic change
    - 1.3 Migration
  2. Labor **demand**
    - 2.1 Technology
    - 2.2 Trade
  3. **Institutions** and policy
    - 3.1 Collective bargaining
    - 3.2 Social norms
    - 3.3 Minimum wages
    - 3.4 Tax system

## What is the impact of labor supply on wages?

Large, controversial literatures on:

- ▶ What is the impact of immigration on native wage inequality?
- ▶ What is the impact of expanding / stagnating access to higher education on wage inequality?

A. Detrended College/High School Wage Differential and Relative Supply, 1963–2005



## Setup

- ▶ Types of workers  $j = 1, \dots, J$   
by level of education, country of birth, ...
- ▶ Cross-section of labor markets  $i = 1, \dots, n$   
e.g., metropolitan areas  
(some papers: time series  $t = 1, \dots, T$ , or panel  $i, t$ )
- ▶ Wages  $w_{ij}$
- ▶ Labor supply  $N_{ij}$

## A typical regression

- ▶ Many papers estimate regressions such as:

$$\log\left(\frac{w_j}{w_{j'}}\right) = \text{controls} + \beta \cdot \log\left(\frac{N_j}{N_{j'}}\right) + \varepsilon_{j,j'},$$

- ▶ possibly instrumenting for labor supply.
- ▶ We will discuss economic models justifying this regression.
- ▶ But don't need to believe models for general interpretation!

### Questions for you

Interpret this regression.

What is the meaning of  $\beta$ ?



## Assumption 1

- ▶ Output  $Y_i$  in region  $i$  is described by an aggregate production function:

$$Y_i = f_i(N_{i1}, \dots, N_{iJ}).$$

- ▶ Marginal productivity theory of wages:

$$w_{ij} = \frac{\partial f_i(N_{i1}, \dots, N_{iJ})}{\partial N_{ij}}$$

- ▶ Justified by competitive, profit maximizing firms

## Reasons marginal productivity theory might not hold

- ▶ If effort / the qualification of applicants depend on wages, employers will not set wage = marginal productivity.
- ▶ If employers face upward sloping labor supply (search frictions!) they depress wages below marginal productivity, acting as a “monopsony.”
- ▶ With search frictions, there is match specific surplus, leaving room for bargaining.
- ▶ Who knows what the marginal productivity is, especially in large, complex firms?
- ▶ Social norms for remuneration.
- ▶ Collective bargaining.
- ▶ Labor markets do not clear.
- ▶ ...

## Assumption 2

- ▶ Constant elasticity of substitution (CES) production function:

$$f_i(N_{i1}, \dots, N_{iJ}) = \left( \sum_{j=1}^J \gamma_j N_{ij}^\rho \right)^{1/\rho}$$

- ▶ Restricts the way different types of labor interact
- ▶  $\rho - 1$ : “inverse elasticity of substitution”  
(we will see why)
- ▶  $\gamma$ : type-specific productivity

## Questions for you

- ▶ Combine assumptions 1 and 2 to derive  $w_{ij}$ .
- ▶ Take the ratio of  $w_{ij}$  and  $w_{ij'}$ .
- ▶ Take logarithms on both sides of the equation.

## Answer: The wage equation

- ▶ Combining assumptions 1 and 2:

$$w_{ij} = \frac{\partial f_i(N_{i1}, \dots, N_{iJ})}{\partial N_{ij}} = \left( \sum_{j'=1}^J \gamma_j N_{ij'}^\rho \right)^{1/\rho-1} \cdot \gamma_j \cdot N_j^{\rho-1}$$

- ▶ Taking ratios:

$$\frac{w_{ij}}{w_{ij'}} = \frac{\gamma_j}{\gamma_{j'}} \cdot \left( \frac{N_{ij}}{N_{ij'}} \right)^{\rho-1}$$

- ▶ Taking logs:

$$\log \left( \frac{w_j}{w_{j'}} \right) = \log \left( \frac{\gamma_j}{\gamma_{j'}} \right) + \beta_0 \cdot \log \left( \frac{N_j}{N_{j'}} \right),$$

where  $\beta_0 = \rho - 1$ .

## Aside: Capital, labor, and the long run evolution of capitalism

- ▶ Aggregate production functions show up in many debates
- ▶ More general form with capital goods  $K$ , technology  $A$ :

$$Y = f(N_1, \dots, N_J, K_1, \dots, K_M, A)$$

- ▶ Wages and rates of return:

$$w_j = \frac{\partial f}{\partial N_j}$$

$$r_m = \frac{\partial f}{\partial K_m}$$

- ▶ Wealth (market value of capital), given interest rate  $r$ :

$$\sum_m \frac{r_m}{r} \cdot K_m$$

## Long standing debates

- ▶ Does technical change lead to increased inequality?
- ▶ What's the distributional impact of international trade / globalization?
- ▶ Does the production function *determine* wages and profits, or leave room for power / collective action?
- ▶ What is the relationship between capital and wealth (capital times market prices)?
- ▶ Does an increase in  $K$  lead to a fall in profit rates?  
cf. Marxist discussions about capitalist crises, imperialism.  
Answer depends on elasticities of substitution, technical change.

## References

- ▶ Impact of migration:  
*Card, D. (2009). Immigration and inequality. The American Economic Review, 99(2):1–21.*
- ▶ Domestic migration of African Americans:  
*Boustan, L. P. (2009). Competition in the promised land: Black migration and racial wage convergence in the north, 1940–1970. The Journal of Economic History, 69(03):755–782.*
- ▶ Technical change:  
*Autor, D. H., Katz, L. F., and Kearney, M. S. (2008). Trends in US wage inequality: Revising the revisionists. The Review of Economics and Statistics, 90(2):300–323.*

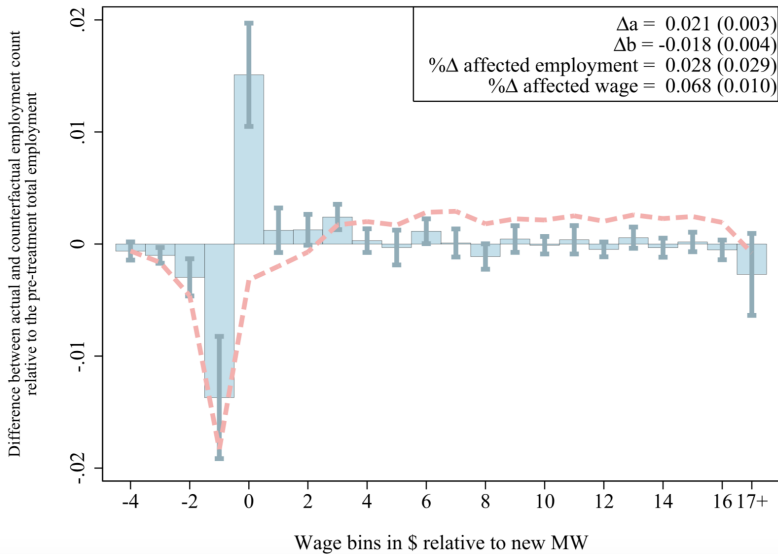


## Minimum wages

- ▶ The competitive model predicts that raising minimum wages decreases employment.
- ▶ What does the evidence say?
- ▶ Many studies use a difference-in-differences design:  
Minimum wage raised in one state of the US but not other, similar states.
- ▶ Compare the changes in employment and earnings in similar states.
- ▶ Majority of recent studies finds no effect on employment.
- ▶ Cengiz et al. (2019) combine the evidence from lots of state minimum wage changes.  
Look at the effect on employment numbers across fine-grained wage cells.

## Cengiz et al. (2019)

- ▶ 138 state-level minimum wage changes between 1979 and 2016 in the United States.
- ▶ Estimate the effect of the minimum wage increase on employment changes by wage bins, relative to the new minimum wage.
- ▶ Compare the number of excess jobs paying at or slightly above the new minimum wage to the missing jobs paying below it to infer the employment effect.
- ▶ The overall number of low-wage jobs remained essentially unchanged over the five years following the increase.



## Monopsony

- ▶ This seems to contradict the competitive model:  
Raising wages yet not changing employment?
- ▶ This consistent empirical finding has renewed interest in monopsony models of the labor market.
- ▶ An employer has monopsony power if their labor supply is not infinitely elastic to the wage.
- ▶ Many reasons (static and dynamic) can lead to upward sloping labor supply for the employer.

## The static monopsony model

- ▶ A firm chooses the number  $L$  of workers it hires.
- ▶ Revenues equal  $R(L)$  when hiring  $L$  workers.
- ▶ In order to hire  $L$  workers, it needs to pay a wage of  $w(L)$ .
- ▶ Competitive case:  $w(L)$  is flat in  $L$ .  
Monopsony power:  $w(L)$  is upward sloping.
- ▶ Firm profits:

$$\pi(L) = R(L) - w(L) \cdot L.$$

## Questions for you

Solve for the profit maximizing wage and employment level in this model.

## Solution

- ▶ First order condition:

$$0 = \pi'(L) = R'(L) - (w(L) + w'(L)L).$$

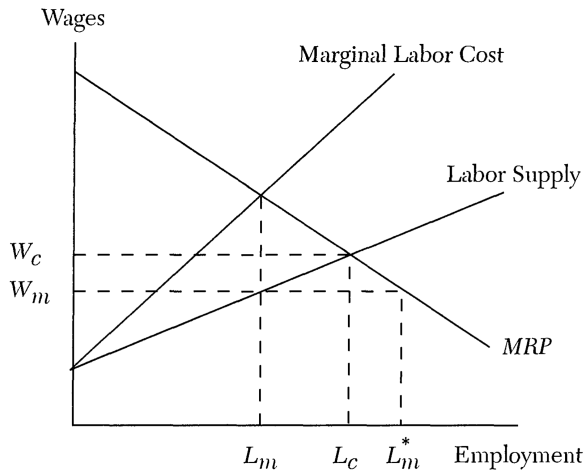
- ▶ Denote the inverse elasticity of labor supply by

$$\eta = \frac{w'(L)L}{w}.$$

- ▶ Rearranging the FOC gives

$$\frac{R'(L) - w(L)}{w} = \eta.$$

- ▶ The marginal revenue product  $R'(L)$  exceeds the wage by a factor of  $\eta$ .
- ▶ Competitive benchmark:  $R'(L) = w(L)$ .



- ▶  $MRP = R'(L)$   
(marginal revenue product)
- ▶ Labor Supply:  $w(L)$
- ▶ Marginal Labor Cost:  
 $(w(L) \cdot L)' = (w(L) + w'(L)L)$

Figure 1. Wage and Employment Determination under Monopsony



## Minimum wage in the monopsony model

- ▶ Now suppose that the firm is not allowed to pay a wage below  $w_m$ .
- ▶ How will it choose  $L$  to maximize profits?

$$\operatorname{argmax}_L (R(L) - \max(w(L), w_m) \cdot L)$$

### Questions for you

Solve for the profit maximizing wage and employment level in the monopsony model when there is a minimum wage.

Hint: Distinguish between 3 different ranges for the minimum wage.

## Solution

3 cases:

1.  $w_m$  is less than the solution of the monopsony FOC:  
 $L^* = \operatorname{argmax}_L (R(L) - w(L) \cdot L).$
2.  $w_m$  is great than the solution of the competitive FOC:  
 $L^* = \operatorname{argmax}_L (R(L) - w_m \cdot L).$
3.  $w_m$  is between these two values:  
Corner solution  $w(L) = w_m.$

Comparative statics:

- ▶ For low  $w_m$ , employment is constant in  $w_m$ .
- ▶ For intermediate  $w_m$ , employment is increasing in  $w_m$ .
- ▶ For high  $w_m$ , employment is decreasing in  $w_m$ .

## Sources of monopsony power

- ▶ Market Concentration
- ▶ Employer Collusion
- ▶ Employer Use of Non-Compete Agreements
- ▶ Search Costs and Labor Market Frictions
- ▶ Regulatory Barriers to Worker Mobility
- ▶ ...

## References

- ▶ *Cengiz, D., Dube, A., Lindner, A., and Zipperer, B. (2019). The Effect of Minimum Wages on Low-Wage Jobs. The Quarterly Journal of Economics, 134(3):1405–1454*
- ▶ *Council of Economic Advisers (2016). Labor market monopsony: Trends, consequences, and policy responses. Council of Economic Advisers Issue Brief, October 2016*
- ▶ *Boal, W. M., Ransom, M. R., et al. (1997). Monopsony in the labor market. Journal of Economic Literature, 35(1):86–112*