

Identification of and correction for publication bias

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Introduction

- Fundamental requirement of science: replicability
- Different researchers should reach same conclusions
- Methodological conventions should ensure this (e.g., randomized experiments)
- Replicability often appears to fail, e.g.
 - Experimental economics (Camerer et al., 2016)
 - Experimental psychology (Open Science Collaboration, 2015)
 - Medicine (Ionnidias, 2005)
 - Cell Biology (Begley et al, 2012)
 - Neuroscience (Button et al, 2013)

Introduction

- Possible explanation: selective publication of results
- Due to:
 - Researcher decisions
 - Journal selectivity
- Possible selection criteria:
 - Statistically significant effects
 - Confirmation of prior beliefs
 - Novelty
- Consequences:
 - Conventional estimators are biased
 - Conventional inference does not control size

Introduction

Literature

Identification of publication bias:

- Good overview:
Rothstein et al. (2006)
- Regression based:
Egger et al. (1997)
- Symmetry of funnel plot (“trim and fill”):
Duval and Tweedie (2000)
- Parametric selection models:
Hedges (1992), Iyengar and Greenhouse (1988)
- Distribution of p-values, parametric distribution of true effects:
Brodeur et al. (2016)

Introduction

Literature

Corrected inference:

- McCrary et al. (2016)

Replication- and meta-studies for empirical part:

- Replication of econ experiments: Camerer et al. (2016)
- Replication of psych experiments: Open Science Collaboration (2015)
- Minimum wage: Wolfson and Belman (2015)
- Deworming: Croke et al. (2016)

Introduction

Our contributions

- 1 Nonparametric **identification of selectivity** in the publication process, using
 - a) Replication studies: Absent selectivity, original and replication estimates should be symmetrically distributed
 - b) Meta-studies: Absent selectivity, distribution of estimates for small sample sizes should be noised-up version of distribution for larger sample sizes
- 2 **Corrected inference** when selectivity is known
 - a) Median unbiased estimators
 - b) Confidence sets with correct coverage
 - c) Allow for nuisance parameters and multiple dimensions of selection
 - d) Bayesian inference accounting for selection
- 3 **Applications** to
 - a) Experimental economics
 - b) Experimental psychology
 - c) Effects of minimum wages on employment
 - d) Effects of de-worming

Outline

- 1 Introduction
- 2 Setup
- 3 Identification
- 4 Bias-corrected inference
- 5 Applications
- 6 Conclusion

Setup

- Assume there is a population of latent studies indexed by i
- True parameter value in study i is Θ_i^*
 - Θ_i^* drawn from some population \Rightarrow empirical Bayes perspective
 - Different studies may recover different parameters
- Each study reports findings X_i^*
 - Distribution of X_i^* given Θ_i^* known
- A given study may or may not be published
 - Determined by both researcher and journal: we don't try to disentangle
- Probability of publication $P(D_i = 1 | X_i^*, \Theta_i^*) = p(X_i^*)$
- Published studies are indexed by j

Setup

Definition (General sampling process)

Latent (unobserved) variables: (D_i, X_i^, Θ_i^*) , jointly i.i.d. across i*

$$\Theta_i^* \sim \mu$$

$$X_i^* | \Theta_i^* \sim f_{X^* | \Theta^*}(x | \Theta_i^*)$$

$$D_i | X_i^*, \Theta_i^* \sim \text{Ber}(p(X_i^*))$$

Truncation: We observe i.i.d. draws of X_j , where

$$l_j = \min\{i : D_i = 1, i > l_{j-1}\}$$

$$\Theta_j = \Theta_{l_j}^*$$

$$X_j = X_{l_j}^*$$

Setup

Example: treatment effects

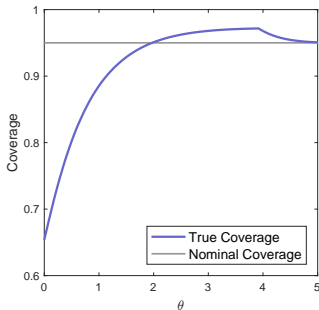
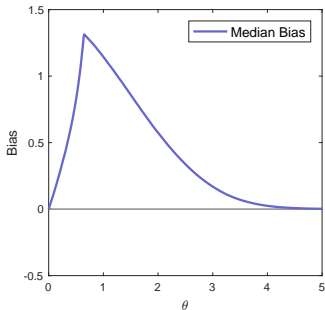
- Journal receives a stream of studies $i = 1, 2, \dots$
- Each reporting experimental estimates X_i^* of treatment effects Θ_i^*
- Distribution of Θ_i^* : μ
- Suppose that $X_i^* | \Theta_i^* \sim N(\Theta_i^*, 1)$
- Publication probability: “significance testing,”

$$p(X) = \begin{cases} 0.1 & |X| < 1.96 \\ 1 & |X| \geq 1.96 \end{cases}$$

- Published studies: report estimate X_j of treatment effect Θ_j

Setup

Example continued – Publication bias



- Left: median bias of $\hat{\theta}_j = X_j$
- Right: true coverage of conventional 95% confidence interval

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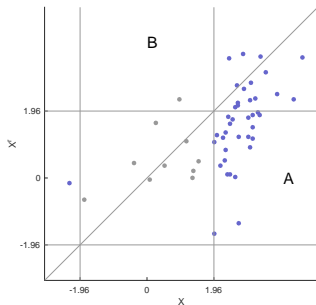
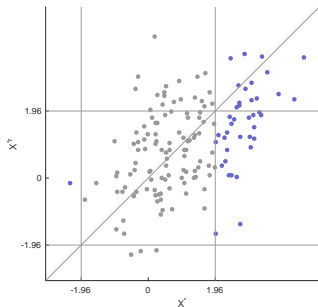
Identification

Identification of the selection mechanism $p(\cdot)$

- Key unknown object in model: publication probability $p(\cdot)$
- We propose two approaches for identification:
 - 1 Replication experiments:
 - replication estimate X^r for the same parameter Θ
 - selectivity operates only on X , but not on X^r
 - 2 Meta-studies:
 - Variation in σ^* , where $X^* \sim N(\Theta^*, \sigma^{*2})$
 - Assume σ^* is (conditionally) independent of Θ^* across latent studies i
 - Standard assumption in the meta-studies literature; validated in our applications by comparison to replications
- Advantages:
 - 1 Replications: Very credible
 - 2 Meta-studies: Widely applicable

Identification

Intuition: identification using replication studies



- Left: no truncation
⇒ areas *A* and *B* have same probability
- Right: $p(Z) = 0.1 + 0.9 \cdot \mathbf{1}(|Z| > 1.96)$
⇒ *A* more likely than *B*

Identification

Approach 1: Replication studies

Definition (Replication sampling process)

- *Latent variables: as before,*

$$\Theta_i^* \sim \mu$$

$$X_i^* | \Theta_i^* \sim f_{X^* | \Theta^*}(x | \Theta_i^*)$$

$$D_i | X_i^*, \Theta_i^* \sim \text{Ber}(p(X_i^*))$$

- *Additionally: replication draws,*

$$X_i^{*r} | X_i^*, D_i, \Theta_i^* \sim f_{X^* | \Theta^*}(x | \Theta_i^*)$$

- *Observability: as before,*

$$l_j = \min\{i : D_i = 1, i > l_{j-1}\}$$

$$\Theta_j = \Theta_{l_j}$$

$$(X_j, X_j^r) = (X_{l_j}^*, X_{l_j}^{*r})$$

Identification

Theorem (Identification using replication experiments)

Assume that the support of $f_{X_i^*, X_i^{*r}}$ is of the form $A \times A$ for some set A . Then $p(\cdot)$ is identified on A up to scale.

Intuition of proof:

- Marginal density of (X, X^r) is

$$f_{X, X^r}(x, x^r) = \frac{p(x)}{E[p(X_i^*)]} \int f_{X^* | \Theta^*}(x | \theta_i^*) f_{X^{*r} | \Theta^*}(x^r | \theta_i^*) d\mu(\theta_i^*)$$

- Thus, for all a, b , if $p(a) > 0$,

$$\frac{p(b)}{p(a)} = \frac{f_{X, X^r}(b, a)}{f_{X, X^r}(a, b)}$$

Identification

Practical complication

- Replication experiments follow the same protocol
⇒ estimate same effect Θ
- But often different sample size
⇒ different variance ⇒ symmetry breaks down
- Additionally: replication sample size often determined based on power calculations given initial estimate
- $p(\cdot)$ is still identified (up to scale):
 - Assume X normally distributed
 - Intuition: Conditional on X, σ , (de-)convolve X^r with normal noise to get symmetry back
 - μ is identified as well

Identification

Further complication

- What if selectivity is based not only on observed X , but also on unobserved W ?
- Would imply general selectivity of the form

$$D_i | X_i^*, \Theta_i^* \sim \text{Ber}(p(X_i^*, \Theta_i^*))$$

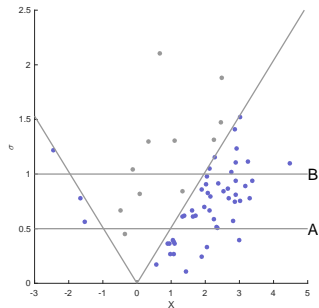
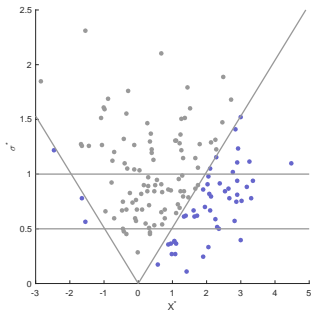
- Again assume normality,

$$X_i^{*r} | \sigma_i, D_i, X_i^*, \Theta_i^* \sim N(\Theta_i^*, \sigma_i^2)$$

- \Rightarrow Solution:
 - Identify $\mu_{\Theta|X}$ from $f_{X^r|X}$ by deconvolution
 - Recover $f_{X|\Theta}$ by Bayes' rule (f_X is observed)
 - This density is all we need for bias corrected inference
- We use this to construct specification tests for our baseline model

Identification

Intuition: identification using meta-studies



- Left: no truncation
⇒ dist for higher σ noised up version of dist for lower σ
- Right: $p(Z) = 0.1 + 0.9 \cdot \mathbf{1}(|Z| > 1.96)$
⇒ “missing data” inside the cone

Identification

Approach 2: meta-studies

Definition (Independent σ sampling process)

$$\sigma_i^* \sim \mu_\sigma$$

$$\Theta_i^* | \sigma_i^* \sim \mu_\Theta$$

$$X_i^* | \Theta_i^*, \sigma_i^* \sim N(\Theta_i^*, \sigma_i^{*2})$$

$$D_i | X_i^*, \Theta_i^*, \sigma_i^* \sim \text{Ber}(p(X_i^* / \sigma_i^*))$$

We observe i.i.d. draws of (X_j, σ_j) , where

$$l_j = \min\{i : D_i = 1, i > l_{j-1}\}$$

$$(X_j, \sigma_j) = (X_{l_j}^*, \sigma_{l_j}^*)$$

Define $Z^* = \frac{X^*}{\sigma^*}$ and $Z = \frac{X}{\sigma}$

Identification

Theorem (Nonparametric identification using variation in σ)

Suppose that the support of σ contains a neighborhood of some point σ_0 . Then $p(\cdot)$ is identified up to scale.

Intuition of proof:

- Conditional density of Z given σ is

$$f_{Z|\sigma}(z|\sigma) = \frac{p(z)}{E[p(Z^*)|\sigma]} \int \varphi(z - \theta/\sigma) d\mu(\theta)$$

- Thus

$$\frac{f_{Z|\sigma}(z|\sigma_2)}{f_{Z|\sigma}(z|\sigma_1)} = \frac{E[p(Z^*)|\sigma = \sigma_1]}{E[p(Z^*)|\sigma = \sigma_2]} \cdot \frac{\int \varphi(z - \theta/\sigma_2) d\mu(\theta)}{\int \varphi(z - \theta/\sigma_1) d\mu(\theta)}$$

- Recover μ from right hand side,
then recover $p(\cdot)$ from first equation

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Bias-corrected inference

- Once we know $p(\cdot)$, can correct inference for selection
- For simplicity, here assume X, Θ both 1-dimensional
- Density of published X given Θ :

$$f_{X|\Theta}(x|\theta) = \frac{p(x)}{E[p(X^*)|\Theta^* = \theta]} \cdot f_{X^*|\Theta^*}(x|\theta)$$

- Corresponding cumulative distribution function: $F_{X|\Theta}(x|\theta)$

Bias-corrected inference

Corrected frequentist estimators and confidence sets

- We are interested in bias, and the coverage of confidence sets
 - Condition on θ : standard frequentist analysis

- Define $\hat{\theta}_\alpha(x)$ via

$$F_{X|\Theta} \left(x | \hat{\theta}_\alpha(x) \right) = \alpha$$

- Under mild conditions, can show that

$$P \left(\hat{\theta}_\alpha(X) \leq \theta | \theta \right) = \alpha \quad \forall \theta$$

- Median-unbiased estimator: $\hat{\theta}_{\frac{1}{2}}(X)$ for θ
- Equal-tailed level $1 - \alpha$ confidence interval:

$$\left[\hat{\theta}_{\frac{\alpha}{2}}(X), \hat{\theta}_{1-\frac{\alpha}{2}}(X) \right]$$

Bias-corrected inference

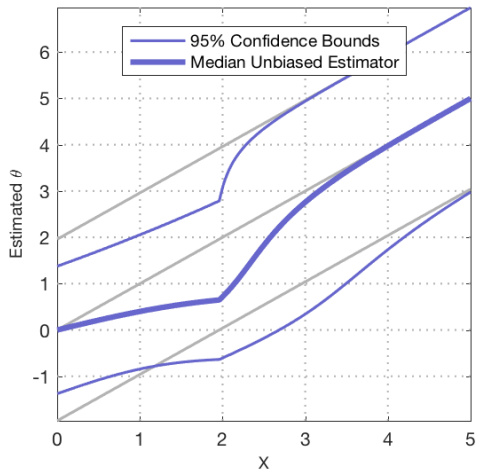
Example: treatment effects

- Let us return to the treatment effect example discussed above
- Again assume $X^*|\Theta^* \sim N(\Theta^*, 1)$ and

$$p(X) = 0.1 + 0.9 \cdot \mathbf{1}(|X| > 1.96)$$

Bias-corrected inference

Example continued – corrected confidence sets for $\beta_p = 0.1$



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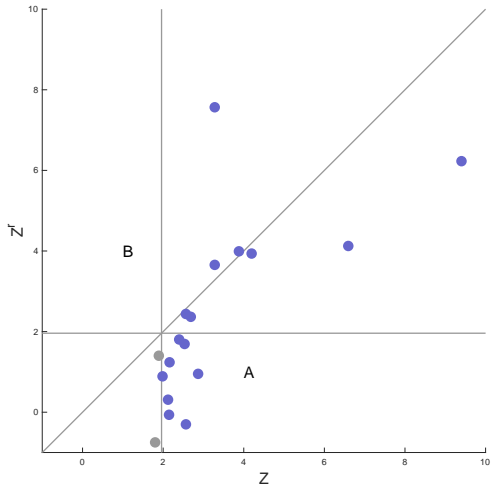
Applications

Replications of Lab Experiments in Economics

- Camerer et al. (2016)
- Sample: all 18 between-subject laboratory experimental papers published in AER and QJE between 2011 and 2014
- Scatterplot next slide:
 - $Z = X/\sigma$: normalized initial estimate
 - $Z^r = X^r/\sigma$: replicate estimate
 - Initial estimates normalized to be positive

Applications

Economics Lab Experiments: Original and Replication Z Statistics



Applications

Economics Lab Experiments: Estimates of Selection model

- Model:

$$|\Theta^*| \sim \Gamma(\kappa, \lambda)$$

$$p(Z) \propto \begin{cases} \beta_p & |Z| < 1.96 \\ 1 & |Z| \geq 1.96 \end{cases}$$

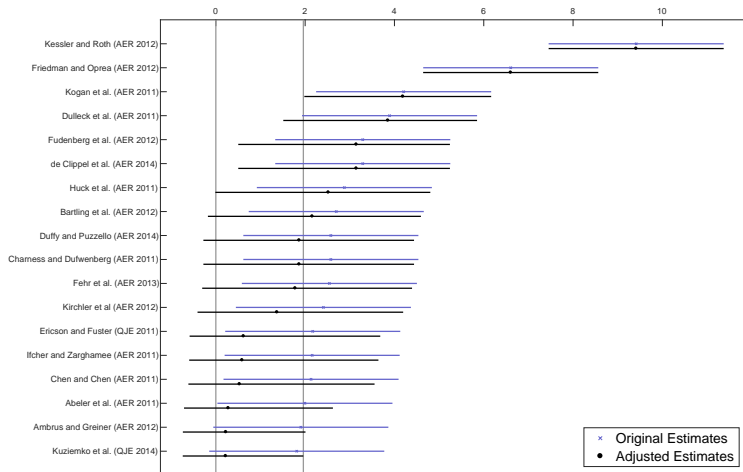
- Estimates:

κ	λ	β_p
0.373	2.153	0.029
(0.266)	(1.024)	(0.027)

- Interpretation: insignificant (at the 5 % level) results about 3% as likely to be published as significant results

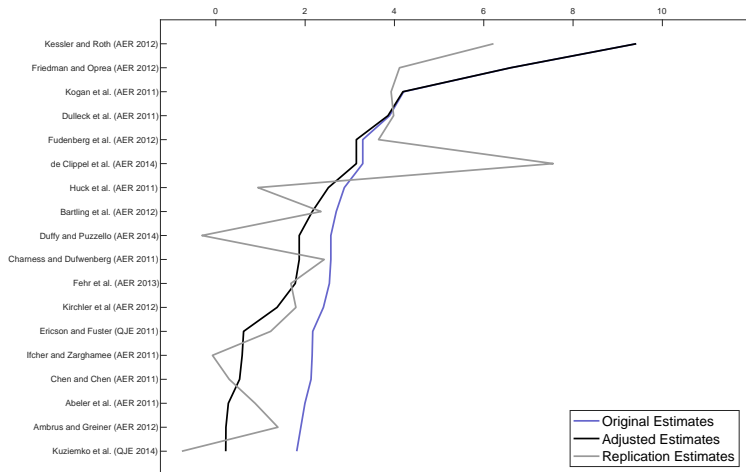
Applications

Economics Lab Experiments: Adjusted Estimates



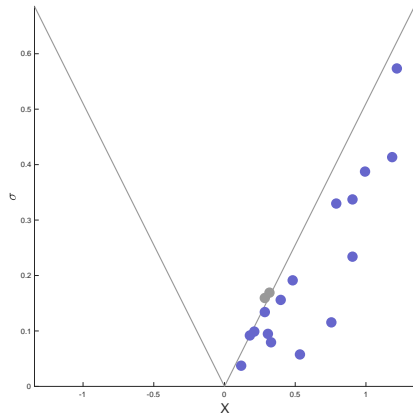
Applications

Economics Lab Experiments: Adjusted Estimates



Applications

Economics Lab Experiments: Meta-study Approach



Applications

Economics Lab Experiments: Meta-study Results

- Model:

$$|\Theta^*| \sim \Gamma(\tilde{\kappa}, \tilde{\lambda})$$

$$\rho(X/\sigma) \propto \begin{cases} \beta_p & |X/\sigma| < 1.96 \\ 1 & |X/\sigma| \geq 1.96 \end{cases}$$

- Recall replication-based estimates:

κ	λ	β_p
0.373	2.153	0.029
(0.266)	(1.024)	(0.027)

- Meta-study based estimates (only β_p comparable):

$\tilde{\kappa}$	$\tilde{\lambda}$	β_p
1.343	0.157	0.038
(1.310)	(0.076)	(0.051)

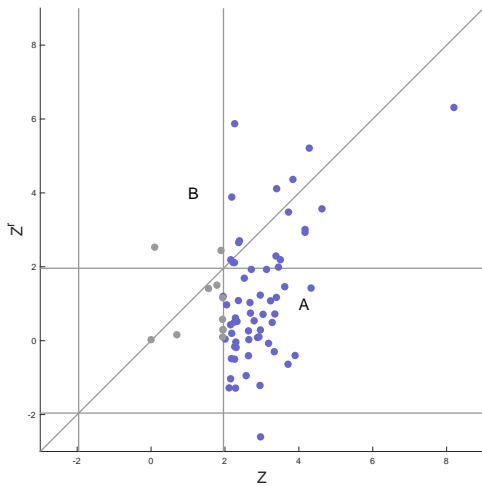
Applications

Replications of Lab Experiments in Psychology

- Open Science Collaboration (2015)
- 270 contributing authors
- Sample: 100 out of 488 articles published 2008 in
 - Psychological Science
 - Journal of Personality and Social Psychology
 - Journal of Experimental Psychology: Learning, Memory, and Cognition
- Some critiques by Gilbert et al. (2016):
 - statistical misinterpretation,
 - not all replication protocols endorsed by original authors
 - ⇒ we re-run estimators on subset of approved replications

Applications

Experiments in Psychology: Original and Replication Z Statistics



Applications

Experiments in Psychology: Estimates of Selection Model

- Model:

$$|\Theta^*| \sim \Gamma(\kappa, \lambda)$$

$$p(Z) \propto \begin{cases} \beta_{p1} & |Z| < 1.64 \\ \beta_{p2} & 1.64 \leq |Z| < 1.96 \\ 1 & |Z| \geq 1.96 \end{cases}$$

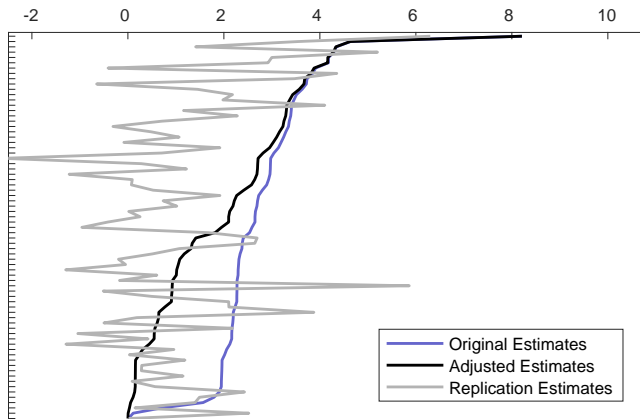
- Estimates:

κ	λ	$\beta_{p,1}$	$\beta_{p,2}$
0.315	1.308	0.009	0.205
(0.143)	(0.334)	(0.005)	(0.088)

- Results insignificant at the 10% level 1% as likely to be published as results significant at 5% level
- Results significant at the 5% level five times as likely to be published as results significant at 10% level

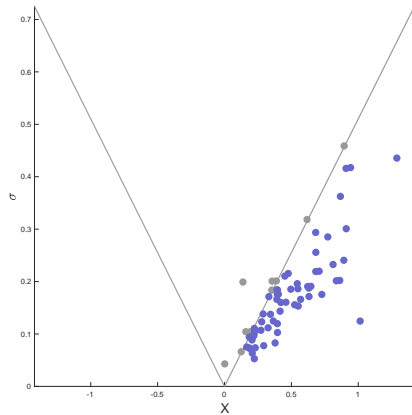
Applications

Original and Replication Z Statistics: Psychology Lab Experiments



Applications

Psychology Lab Experiments: Meta-studies Approach



Applications

Psychology Lab Experiments: Estimates of Meta-studies Selection Model

- Model:

$$|\Theta^*| \sim \Gamma(\tilde{\kappa}, \tilde{\lambda})$$

$$p(Z) \propto \begin{cases} \beta_{p1} & |Z| < 1.64 \\ \beta_{p2} & 1.64 \leq |Z| < 1.96 \\ 1 & |Z| \geq 1.96 \end{cases}$$

- Recall replication-based estimates:

κ	λ	$\beta_{p,1}$	$\beta_{p,2}$
0.315	1.308	0.009	0.205
(0.143)	(0.334)	(0.005)	(0.088)

- Meta-study based estimates (only β_p comparable):

$\tilde{\kappa}$	$\tilde{\lambda}$	$\beta_{p,1}$	$\beta_{p,2}$
0.974	0.153	0.017	0.306
(0.549)	(0.053)	(0.009)	(0.135)

Applications

Psychology Lab Experiments: Approved Replications

- 67 studies
- Replication-based estimates:

κ	λ	$\beta_{p,1}$	$\beta_{p,2}$
0.490	1.159	0.017	0.365
(0.268)	(0.402)	(0.011)	(0.165)

- Meta-study based estimates:

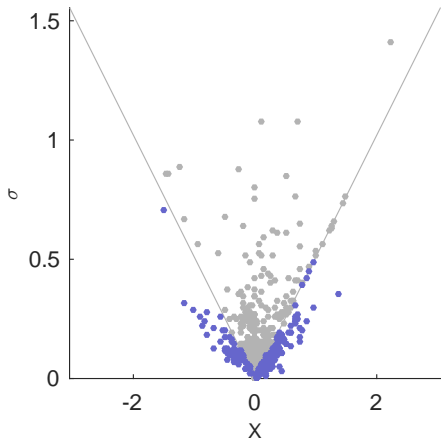
$\tilde{\kappa}$	$\tilde{\lambda}$	$\beta_{p,1}$	$\beta_{p,2}$
0.634	0.198	0.022	0.440
(0.502)	(0.078)	(0.014)	(0.217)

- β_p estimates larger than those in full dataset

Applications

Meta-study of the Effect of Minimum Wages on Employment

- Wolfson and Belman (2015)
- Elasticity of employment w.r.t. the minimum wage
 $X > 0 \Leftrightarrow$ negative employment effect
- 1000 estimates from 37 studies using U.S. data that were circulated after 2000, either as articles in journals or as working papers
- For some: more than 1 estimate per study



Estimates of selection model

- Model:

$$\Theta^* \sim \bar{\theta} + t(v) \cdot \tilde{\tau}$$
$$\rho(X/\sigma) \propto \begin{cases} \beta_{p1} & X/\sigma < -1.96 \\ \beta_{p2} & -1.96 \leq X/\sigma < 0 \\ \beta_{p3} & 0 \leq X/\sigma < 1.96 \\ 1 & X/\sigma \geq 1.96 \end{cases}$$

- Recall $X > 0 \Leftrightarrow$ negative employment effect.
- Estimates:

$\bar{\theta}$	$\tilde{\tau}$	\tilde{v}	$\beta_{p,1}$	$\beta_{p,2}$	$\beta_{p,3}$
0.018	0.019	1.303	0.697	0.270	0.323
(0.009)	(0.011)	(0.279)	(0.350)	(0.111)	(0.094)

- Selection in favor of significant effects, negative effects.

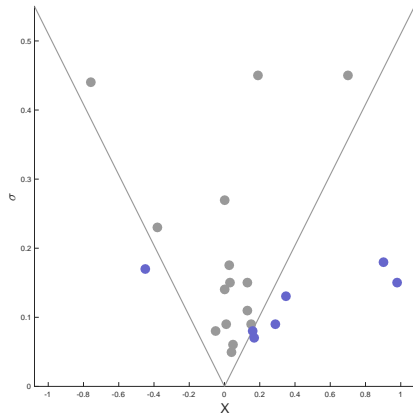
Applications

Meta-Study of the Effects of Deworming

- Croke et al. (2016)
- Follow procedures outlined in the “Cochrane Handbook for Systematic Reviews of Interventions”
- Randomized controlled trials of deworming that include child body weight as an outcome
- 22 estimates from 20 studies

Applications

Meta-Study of the Effects of Deworming



Applications

Deworming: Estimates of selection model

- Model:

$$\Theta^* \sim N(\bar{\theta}, \tau^2)$$
$$\rho(X) \propto \begin{cases} \beta_p & |X/\sigma| < 1.96 \\ 1 & |X/\sigma| \geq 1.96 \end{cases}$$

- Estimates:

$\bar{\theta}$	$\tilde{\tau}$	β_p
0.190	0.343	2.514
(0.120)	(0.128)	(1.869)

Conclusion

- Selectivity in the publication process is a potentially serious problem for statistical inference.
- We non-parametrically identify the form of selectivity:
 - Using replication studies:
Original and replication estimates would be symmetrically distributed, absent selectivity
 - Using meta-studies:
Under an independence assumption, higher-variance estimate distribution would be noised-up version of lower-variance estimate distribution, absent selectivity

Conclusion

- Easy correction for selectivity, if form is known:
 - Median unbiased estimators
 - Equal-tailed confidence sets with correct coverage
- Empirical findings:
 - Selectivity on significance in experimental economics, experimental psychology
 - Selectivity towards (negative) significant employment effects in minimum wage literature
 - Noisy estimates in meta-study for de-worming

Thank you!